## SetsH

## Question 1 (2016)



## Question 2 (2013)

(b) In a class of 30 students, 20 study Physics, 6 study Biology and 4 study both Physics and Biology.
(i) Represent the information on the Venn Diagram.

A student is selected at random from this class.
The events E and F are:
E: The student studies Physics
F: The student studies Biology.

(ii) By calculating probabilities, investigate if the events E and F are independent.

$$
\begin{aligned}
& P(E \cap F)=\frac{4}{30} \\
& P(E) \times P(F)=\frac{20}{30} \times \frac{6}{30}=\frac{4}{30} \\
& P(E \cap F)=P(E) \times P(F) \quad \Rightarrow \quad E \text { and } F \text { are independent events }
\end{aligned}
$$

Question 1
The events $A$ and $B$ are such that $P(A)=0.7, P(B)=0.5$ and $P(A \cap B)=0.3$.
(a) Find $P(A \cup B)$.

$$
\begin{aligned}
P(A \cup B) & =P(A)+P(B)-P(A \cap B) \\
& =0.7+0.5-0.3 \\
& =0.9
\end{aligned}
$$

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(b) Find $P(A \mid B)$.

$$
\begin{aligned}
P(A \mid B) & =\frac{P(A \cap B)}{P(B)} \\
& =\frac{0.3}{0.5} \\
& =0.6
\end{aligned}
$$

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(c) State whether $A$ and $B$ are independent events and justify your answer

If $A$ and $B$ are independent events then $P(A \cap B)=P(A) P(B)$.
Here, $P(A \cap B)=0.3$ but $P(A) P(B)=(0.7)(0.9)=0.63$.
So $A$ and $B$ are NOT independent events.

