

Q1's :

Negative displacement 2002 Q1 a^(*), ~~2003 Q1a~~

passing posts 2002 Q1 b, 2003 Q1 a^(*)
2011 Q1 a,

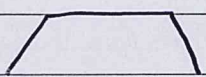
'just catches', closest distance 2003 Q1 b^(*) (!)

forces / penetrates 2004 Q1(b)^(*), 2005 Q1(b)^(*)

Distance Vs Displacement 2004 Q1(a)^(*), 2008 Q1(a)^(*)

Trains passing / lengths 2006 Q1(b)^(*)

Accel / Decel / ratios 2006 Q1(a) 2009 Q1(b)



2007 Q1(b) 2011 Q1(b)^(*)

In 2nd second, in 5th second !! 2007 Q1(a)^(*)

watch \dot{b} !

Answer Q!!!

Answer part (iii) even if you couldn't do ii)

Do 2012 Q1 (b)

time - think which has been travelling longer
and rem: $\underline{t+2}$, t \underline{t} , $t-2$

2010 Q1 (b) = hard

- * Area under curve is distance travelled
- * can only deal with each period of acceleration individually - if accel changes \Rightarrow new $u, v, a, t,$

* Average Speed = $\frac{\text{Total distance}}{\text{Total time}}$

* Uniform Speed \Rightarrow No acceleration 2004(b)
 \Rightarrow force overall = 0 !

Distance
 * in the 7th sec
 = distance for 1st 7sec - distance for 1st 6 sec's

2003 (a) ^{passing posts} and (b) (just catches)

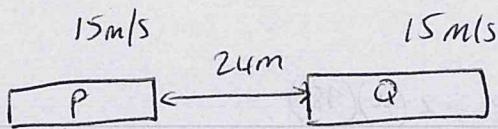
2004 (a) and (b) (caravan, force, Uniform speed)
 distance vs displacement

2002 (a) easy ^{displacement} (b) passing posts algebra

2001 (a) Do (b) 2 cars (hard) do

1998 (a) Algebra ($5v/6$) (b) Do

Q 1
2014
(a)



2014 Q 1

In time t :

P:	Q:
$u = 15$	$u = 15$
$v =$	$v =$
$a = -4$	$a = -5$
$s = 15t - 2t^2$	$s = 15t - 2.5t^2$
$t = t$	$t = t$

~~S_P~~ $S_Q + 24 - S_P = 15t - 2.5t^2 + 24 - 15t + 2t^2 - 0.5t^2 + 24$

(ii)

$u = 15$	$u = 15$
$v = 0$	$v = 0$
$a = -4$	$a = -5$
$s = 15t - 2t^2$	$s =$
$t = t$	$t = t$

$0 = 225 - 8s$
 $s = \frac{225}{8}$

$0 = 225 - 10s$
 $225 = 10s$

$\frac{225}{10} + \frac{24}{10} - \frac{225}{8}$

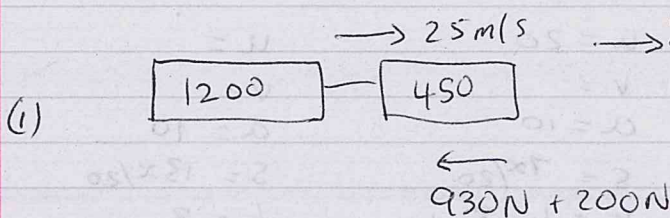
463

$\frac{465}{10} - \frac{225}{8} = 18.375$

$P = \frac{W}{t} = \frac{F \cdot d}{t} = Fv$

$\frac{50000}{25} = \frac{F}{2000N}$

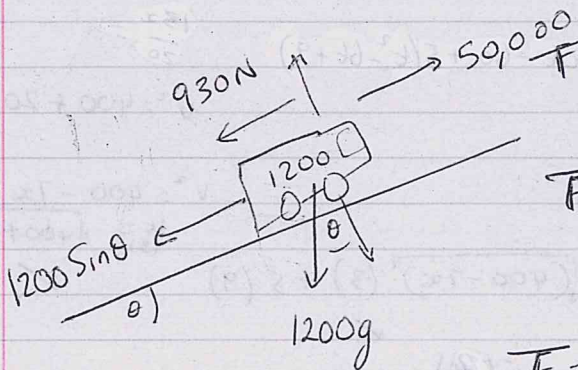
(b)



$a = \frac{F}{m} = \frac{2000 - 1130}{1650}$

$= \frac{29}{55}$
 $= 0.527$

(ii)



$F - 1200g \sin \theta = 1200a$ (o)

$F - 1200g_n = 1200a$ (o)

$F = \frac{50,000}{v}$

$T = \frac{50000}{v}$

$v = \frac{50000}{2106} = 23.74 \text{ m/s}$

2010: (Q1)

$$u = 14$$

$$v = 0$$

$$0^2 = 196 + 2(a)(98)$$

(i)

$$a =$$

$$s = 98$$

$$t =$$

$$a = \frac{-196}{196} = -1 \text{ m/s}^2$$

(ii)

In 1 sec car travels 14m. It is now 84m from traffic light.

$$u = 14$$

$$v = 0$$

$$a =$$

$$s = 84$$

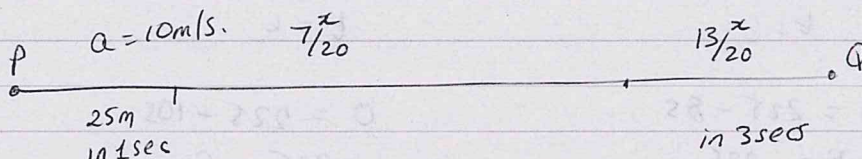
$$t =$$

$$0^2 = 196 + 2a(84)$$

$$-196/168 = -1.17 \text{ m/s}^2$$

20

(b.)



$$u = 20$$

$$v =$$

$$a =$$

$$s = 25$$

$$t = 1$$

$$s = 20 + \frac{a}{2}$$

$$s = \frac{a}{2}$$

$$a = 10 \text{ m/s}^2$$

travels P \rightarrow Q in t secs

$7x/20$ in $t-3$ secs

$13x/20$ in 3 secs.

$$u = 20$$

$$v =$$

$$a = 10$$

$$s = x$$

$$t = t$$

$$u = 20$$

$$v =$$

$$a = 10$$

$$s = 7x/20$$

$$t = t-3$$

$$u =$$

$$v =$$

$$a = 10$$

$$s = 13x/20$$

$$t = 3$$

$$v^2 = 400 + 20\left(\frac{7x}{20}\right)$$

$$v^2 = 400 - 7x$$

$$u_{(3)} = \sqrt{400 + 7x}$$

$$\frac{13}{20} = \frac{\sqrt{(400 - 7x)}(3) + 5(9)}{20}$$

$$13x = 60\sqrt{400 - 7x} + 45(20)$$

$$(13x - 900)^2 = 3600(400 - 7x)$$

$$169x^2 - 23400x + 810000 = 1440000 + 25200x$$

$$169x^2 - 48600x - 630000 = 0 \quad \leftarrow x = 300 \text{ m.}$$

2013:

$u = 44.1$

(a)

$v =$

$a = -9.8$

$s = 39.2$

$t = ?$

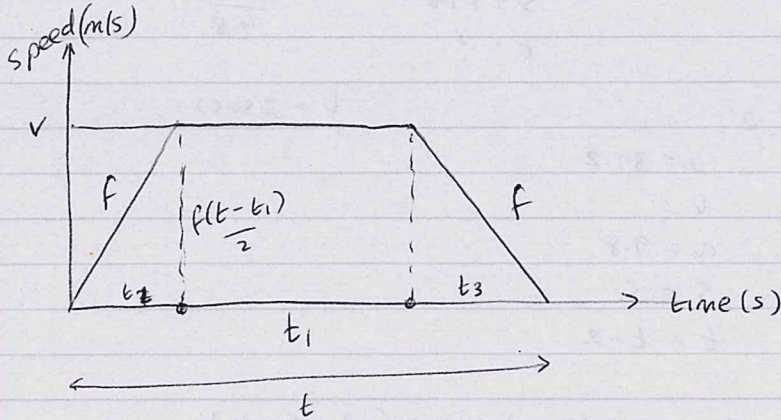
$39.2 = 44.1t - 4.9t^2$

$8 = 9t - t^2$

$t^2 - 9t + 8 = 0$

$(t-1)(t-8) \quad t=1 \quad t=8, \text{ Ans} = 7 \text{secs}$

(b)



$u = 0$

$v = v$

$a = f$

$s =$

$t = t_2$

$v = ft_2$

$u = v$

$v = 0$

$a = -f$

$s =$

$t = t_3$

$0 = v - ft_3$

$v = ft_3$

$t_2 = t_3$

So $t_2 = t_3 = \frac{t-t_1}{2}$

$\therefore v = f \left(\frac{t-t_1}{2} \right)$

$d = \frac{1}{2} \left(\frac{t-t_1}{2} \right) \left(\frac{t-t_1}{2} \right) f + \frac{1}{2} \left(\frac{t-t_1}{2} \right) \left(\frac{t-t_1}{2} \right) f + f \left(\frac{t-t_1}{2} \right) t_1$

$d = \frac{(t-t_1)^2}{4} f + f \left(\frac{t-t_1}{2} \right) t_1 =$

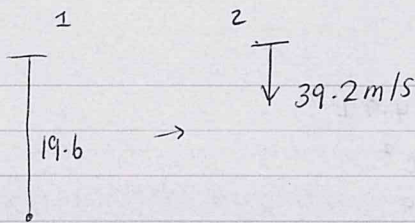
$d = \left(t^2 - 2tt_1 + t_1^2 \right) f + 2f(t_1 t_1)$

$\frac{4d}{f} = t^2 - t_1^2$

$\sqrt{t^2 - \frac{4d}{f}} = t_1^2$

2012

Q1 (a)



Particles collide when $S_1 = S_2$

find time to fall 19.6m : $u = 0$ $19.6 = \frac{9.8 t^2}{2}$
 $v =$
 $a = 9.8$ $t^2 = \frac{39.2}{9.8} = 4$
 $S = 19.6$
 $t = ?$

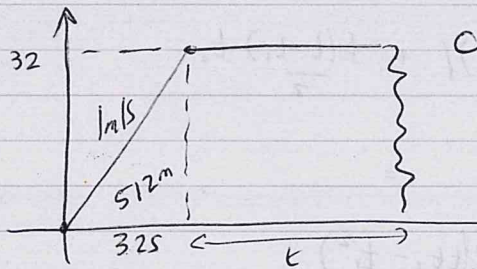
1:	2:
$u = 0$	$u = 39.2$
$v =$	$v =$
$a = 9.8$	$a = 9.8$
$S = S$	$S = S$
$t = t$	$t = t - 2$

$t = 2 \text{ secs}$

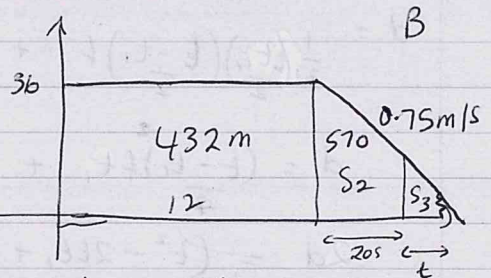
$S = 4.9t^2$ $S = 39.2(t-2) + 4.9(t^2 - 4t + 4)$
 $4.9t^2 = 39.2t - 78.4 + 4.9t^2 - 19.6t + 19.6$
 $4.9t^2 = 4.9t^2 + 19.6t - 58.8$
 $t = \frac{58.8}{19.6} = 3 \text{ secs}$

$d = 4.9(3)^2 = 44.1 \text{ m}$

(b.)



$u = 0$ $32 = 0 + (1)t$
 $v = 32$ $32^2 = 0 + 2(1)S$
 $a = 1$ $S = 512 \text{ m}$
 $S = ?$ $t = 32 \text{ s}$



In 32s Bus travels $36(12) + S_2$
 $u = 36$ $S = 36(20) - (375)(400)$
 $v =$ $S = 570$
 $a = 0.75$ $V = 36 + 0.75(20)$
 $S = ?$ $V = 21 \text{ m/s}$
 $t = 20$

In 32sec $S_{\text{Car}} = 512 \text{ m}$

In 32sec $S_{\text{Bus}} = 570 \text{ m} + 432 \text{ m}$

Bus + Car : 1514 m . they overtake when $S_B + S_C = 1914$

$1914 = 512 + 32t + 432 + 570 + S_3$ find S_3 : $u = 21$

$1914 = 512 + 32t + 432 + 570 + 21t - \frac{3t^2}{8}$
 $400 = 32t - \frac{3t^2}{8}$ $3t^2 - 424t + 3200 = 0$
 $t = 8, t = \frac{400}{3}$

$v =$
 $a = -0.75$
 $S = 21t - \frac{3}{8}t^2$
 $t = t$

After 48secs: 8secs Car: $32(8) = 256$

Bus: $u(t=8) = 21 + 0.75(8) = 15 \text{ m/s}$ Overall $t = 32 + 8 = 40$

$u = 15$ $a = -0.75$ $S = ?$ $t = 8 \Rightarrow 96 \text{ m}$

Q1's:

2013 (a.) 1

(*) $S =$ displacement (for upward throws)

$u = 44.1$

Quadratics

$v = 39.2 = 44.1t - 4.9t^2$ (*) divide by 4.9

$a = -9.8$

check

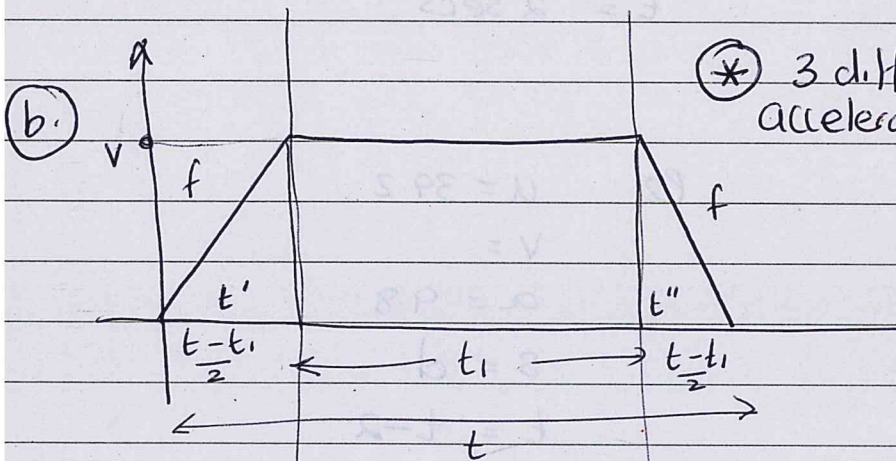
$S = 39.2 \quad t^2 - 9t + 8 = 0$

$t = (t-8)(t-1) \quad t = 8 \text{ sec} \quad t = 1 \text{ sec}$

Check you have

Ans: $8-1 = 7 \text{ secs}$

(*) Answered the Q being asked or (-5 marks)



(*) 3 different accelerations $t' = t'' \Rightarrow t - t_1 = 2t'$

$t' = \frac{t-t_1}{2}$

(*) Area under curve = distance

$u = 0$

(*) Average speed =

$v = v$

$v = 0 + f \left(\frac{t-t_1}{2} \right)$

$\frac{\text{total distance}}{\text{total time}}$

$a = f$

$s =$

$t = \frac{t-t_1}{2}$

(*)

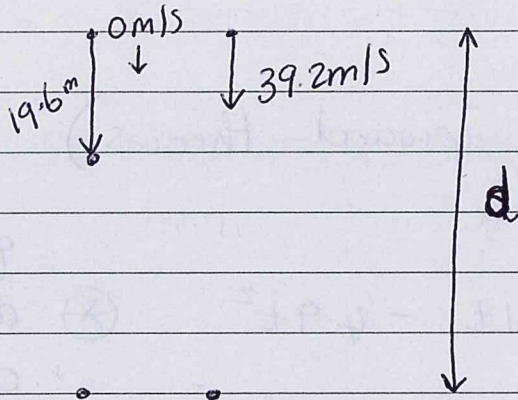
$d = 2 \left(\frac{t-t_1}{4} \right) v + t_1 v \Rightarrow d = \frac{2(t-t_1)}{4} \cdot f (t-t_1) + \frac{t_1(t-t_1)}{2}$

$d = f \frac{(t^2 - 2tt_1 + t_1^2)}{4} + \frac{2t_1 f (t-t_1)}{4} \Rightarrow \frac{4d}{f} = t^2 - t_1^2$

$4d = ft^2 - 2ftt_1 + ft_1^2 + 2t_1f - 2t_1^2f \Rightarrow t^2 - \frac{4d}{f} = t_1^2$

2012

1(a.)



(*) $t+2$ or $t-2$?

think which has been travelling longer and

rem t , $\underline{t+2}$

longer $\rightarrow \underline{t}$ $t-2$

P1: $u=0$

$v=$

$a=9.8$

$s=19.6$

$t=?$

$19.6 = 0 + 4.9t^2$

$t^2 = 4$

$t = 2 \text{ secs}$

P1: $u=0$

$v=$

$a=9.8$

$s=d$

$t=t$

P2

$u=39.2$

$v=$

$a=9.8$

$s=d$

$t=t-2$

$d = 4.9t^2 = 39.2(t-2) + 4.9(t^2 - 4t + 4)$

$4.9t^2 = 39.2t - 78.4 + 4.9t^2 - 19.6t + 19.6$

$19.6t + 19.6 - 78.4 = 0$

$19.6t = 58.8$

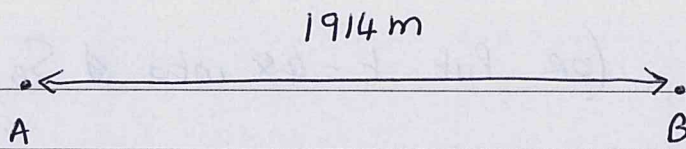
$t = 3 \text{ secs}$

$d = 4.9t^2 = 44.1 \text{ m}$

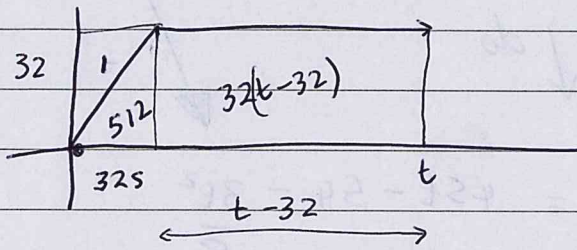
(*) Answer the Φ

* DU

1 (b.)

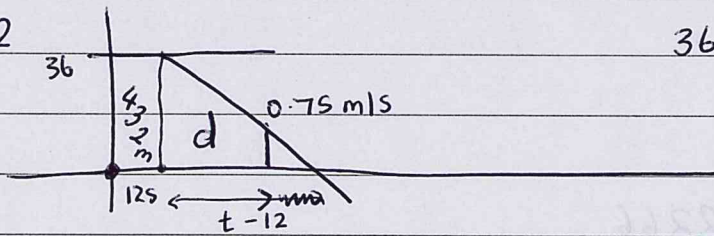


Car 1



$$\begin{aligned}
 u &= 0 & 32^2 &= 0^2 + 2s \\
 v &= 32 & \Rightarrow s &= 512 \\
 a &= 1 \\
 s &= & 32 &= 1t \\
 t &= & 32s &= t
 \end{aligned}$$

Part 2



$$36 \text{ m/s for } 12 \text{ s} \Rightarrow 432 \text{ m}$$

$$\begin{aligned}
 S_C + S_B &= 1914 \text{ when they meet.} \\
 t &= \text{time}
 \end{aligned}$$

$$\begin{aligned}
 S_C &= 512 + 32t - 1024 \\
 &= 32t - 512
 \end{aligned}$$

$$S_B = 432 + d$$

* Part (ii) can be done whether or not you get part (i)

$$d = ? \quad u = 36 \quad d = 36t - 432 - 0.375(t^2 - 24t + 144)$$

$$v =$$

$$a = -0.75 \quad d = 45t - 486 - \frac{3t^2}{8} \quad (\text{*) Don't (x8)!}$$

$$s = d$$

$$t = t - 12$$

$$\therefore S_B = 432 - 486 + 45t - \frac{3t^2}{8}$$

$$S_B + S_C = 32t - 512 + 45t - \frac{3t^2}{8} - 54 = 45t - 54 - \frac{3t^2}{8}$$

$$= 1914 = -\frac{3t^2}{8} - 566 + 77t \Rightarrow 3t^2 - 616t + 1980 = 0$$

$$t = 1653 \text{ or } t = 40$$

48-40
(ii) 8 seconds later? (or Put $t=48$ into S_B, S_C and subtract)

$32(8) =$ distance travelled by car

Complicated/messy \downarrow do

$$S_C = 32(8) - 512$$

$$S_B = 45t - 54 - \frac{3t^2}{8}$$

$$1536$$

$$1242$$

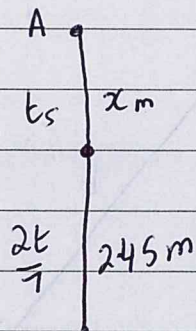
$$- 512$$

$$1024 \text{ m}$$

$$1024 + 1242 = 2266$$

$$2266 - 1914 = 352 \text{ m}$$

2011
Q1: (a)



(*) look at $A \rightarrow B$
look at $A \rightarrow C$?

get Simultaneous Eqn.

look $A \rightarrow B$

$$u = 0$$

$$u = 0$$

$$v =$$

$$v =$$

$$a = 9.8$$

$$a = 9.8$$

$$s = x$$

$$s = x + 2.45$$

$$t = t$$

$$t = t + \frac{2t}{7} = \frac{9t}{7}$$

$$x = 4.9t^2 \quad \checkmark$$

$$x + 2.45 = 4.9 \left(\frac{81t^2}{49} \right)$$

$$49x + 120.05 = 396.9t^2 \quad (396.9t^2)$$

$$240.1t^2 + 120.05 = 396.9t^2$$

$$120.05 = 156.8t^2$$

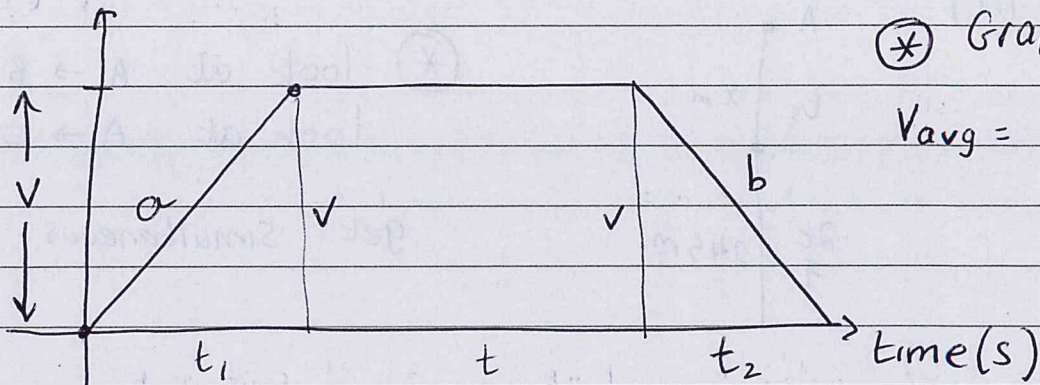
$$\frac{49}{64} = t^2 \quad t = \frac{7}{8} \text{ secs}$$

2011 (b)

(*) Def do!!!

(*) Graph!

(i)



$$V_{avg} = \frac{3v}{4}$$

(*) Average speed = $\frac{\text{Total distance}}{\text{Total time}} = \frac{3v}{4}$

(ii)

$$\text{Total time} \times \frac{3v}{4} = \text{Total distance}$$

$$\text{Total time} = \frac{4(\text{Total distance})}{3v} = t + t_1 + t_2$$

$$\text{Total distance} = \frac{vt_1}{2} + \frac{vt_2}{2} + vt$$

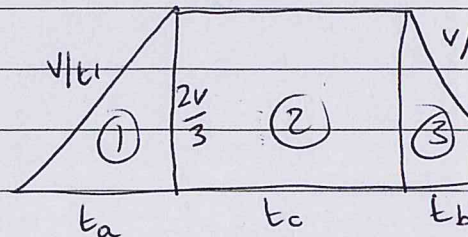
$$\text{So } t + t_1 + t_2 = \frac{4v}{3v} \left(\frac{t_1}{2} + \frac{t_2}{2} + t \right)$$

$$3t + 3t_1 + 3t_2 = 2t_1 + 2t_2 + 4t$$

$$t_1 + t_2 = t$$

(iii) $u=0$
 $v=v$
 $a=a$ $v=at_1$
 $s=vt_1/2$ $v=a$
 $t=t_1$ t_1

$$b = \frac{v}{t_2}$$



(3) $u=v/t_2$
 $\text{total time} = v = 2v/3$
 $a = v/t_2$
 $s =$
 $t = t_b$

(2) $u=0$
 $v=2v/3$
 $a=v/t_1$
 $s =$
 $t = t_a$

$$t_a = \frac{2t_1}{3} \quad t_b = \frac{2t}{3}$$

(iii)

$$\text{Total distance} = \frac{1}{2}(t_a) \frac{2v}{3} + \frac{1}{2}(t_b) \frac{2v}{3} + t_c \cdot \frac{2v}{3}$$

$$= v \left(\frac{t_a}{3} + \frac{t_b}{3} + \frac{2t_c}{3} \right) = v \left(\frac{2t_1}{9} + \frac{2t_2}{9} + \frac{6t_c}{9} \right)$$

$$= \frac{v}{9} (2(t_1+t_2) + 6t_c) = \frac{v}{9} (2t + 6t_c)$$

$$\text{From (ii) total distance} = \frac{vt_1}{2} + \frac{vt_2}{2} + vt$$

$$= \frac{v(t_1+t_2)}{2} + vt = \frac{vt}{2} + vt = \frac{3vt}{2}$$

same distance in (ii) and (iii) so:

$$\frac{3vt}{2} = \frac{v}{9} (2t + 6t_c)$$

$$27t = 4t + 12t_c \Rightarrow t_c = \frac{23t}{12}$$

$$\text{Total time} = \frac{23t}{12} + t_a + t_b = \frac{23t}{12} + \frac{2(t_1+t_2)}{3}$$

$$= \frac{23t}{12} + \frac{2t}{3} = \frac{31t}{12}$$

2010

① (a.) $u = 14 \text{ m/s}$

$v = 0$

~~$0 = 14 + at$~~

$a = ?$

$0^2 = 14^2 + 2a(98)$

$S = 98$

$a = -1 \text{ m/s}^2$

$t =$

if driver hesitates 1s he travels another 14 m

$u = 14$

$0^2 = 14^2 + 2a(84)$

$v = 0$

$0 = 196 + 168a$

⊗ be careful

$a = ?$

$a = \frac{196}{168} = 1.16 \text{ secs}$

$S = 84$

168

$t =$

①

(b.)

20 m/s

1 sec

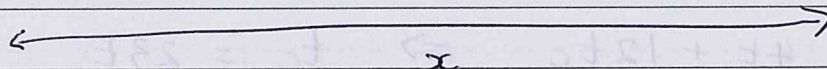
3 sec

25 m

$\frac{13x}{20}$

P

⊗ look at whole part



$u = 20$

$25 = 20 + \frac{a}{2}$

$a = 10 \text{ m/s}$

$u = \sqrt{400 + 7x}$

$v =$

$v =$

$a =$

$a = 10$

$S = 25$

$S = \frac{13x}{20}$

$t = 1$

$t = 3$

$u = 20$

$v^2 = 400 + 20 \cdot \frac{7x}{20}$

$\frac{13x}{20} = 3 \sqrt{400 + 7x} + 5(9)$

$v =$

$a = 10$

$S = 7x/20$

$v^2 = 400 + 7x$

$\frac{13x - 900}{20} = \sqrt{400 + 7x}$

$t =$

$169x^2 - 23400x + 810000 = 40000$
 $169x^2 - 26200x + 850000 = 0$

$$\frac{13x-900}{60} = \sqrt{400+7x}$$

$$\frac{169x^2 - 23400x + 810000}{3600} = 400 + 7x$$

$$169x^2 - 23400x + 810000 = 1440000 + 25200x$$

$$169x^2 - 48600x - 630000 = 0$$

$$\text{Ans: } x = 300 \text{ m.}$$

2009 Q1(a)

P1

P2

$$u = u$$

$$u = 0$$

$$v = v$$

$$v = v$$

$$a = -9.8$$

$$a = 9.8$$

$$s = s_{rp}$$

$$s = s_{rq}$$

$$t = 2$$

$$t = 2$$

$$v = u - 9.8(2)$$

$$v = 0 + 9.8(2)$$

$$w = v + 19.6$$

$$v = 19.6$$

$$s_{rp} = (v + 19.6) \cdot 2 - 4.9(4)$$

$$\rightarrow \text{So } 19.6 = \frac{s_{rp} - 19.6}{2}$$

$$s_{rp} = 2v + 39.2 - 19.6$$

$$s_{rp} = 2v + 19.6$$

$$39.2 = s_{rp} - 19.6$$

$$58.8 = s_{rp}$$

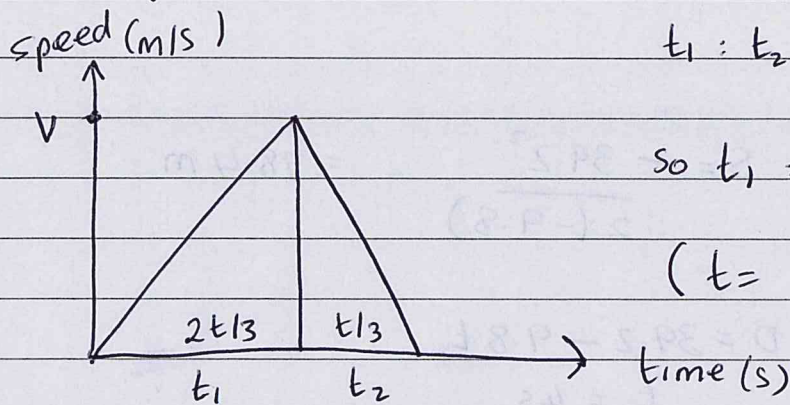
$$v = \frac{s_{rp} - 19.6}{2}$$

$$P2: s_{rq} = \left(\frac{u+v}{2}\right)t$$

$$s_{rq} = \left(\frac{0 + 19.6}{2}\right) \cdot 2 = 19.6$$

$$\text{So } \frac{s_{rp}}{s_{rq}} = \frac{58.8}{19.6} = 3$$

2009 Q1 (b)



$$t_1 : t_2 = 2 : 1$$

$$\text{so } t_1 = 2t/3, t_2 = t/3$$

(t = total time)

$$\frac{\text{Total distance}}{\text{total time}} = \frac{d}{t} = \sqrt{\frac{d}{3}} \Rightarrow \frac{d^2}{t^2} = \frac{d}{3}$$

$$d = \frac{t^2}{3}$$

$$\text{also } d = \text{area of } \triangle = \frac{1}{2}(t)V$$

$$u = 0$$

$$v = v \quad v = 0 + f \cdot \frac{2t}{3}$$

$$a = f$$

$$S =$$

$$v = \frac{2ft}{3}$$

$$\text{so } d = \frac{1}{2}(t)\left(\frac{2ft}{3}\right)$$

$$t = 2t/3$$

$$d = \frac{2ft^2}{3}$$

$$\text{since } \frac{t^2}{3} = d \Rightarrow d = 2fd$$

$$\frac{d}{d} = f = 1$$

(*) (*) check times $\int \int$

displacement
!!!
not distance

2008 : Q1 (a)

$$u = 39.2$$

$$v = 0$$

$$a = -9.8$$

$$s =$$

$$t =$$

$$s = \frac{-39.2^2}{2(-9.8)} = 78.4 \text{ m}$$

$$2(-9.8)$$

$$0 = 39.2 - 9.8t$$

$$t = 4 \text{ s}$$

so, for final sec:

OR

$$u = 39.2$$

$$v =$$

$$a = -9.8$$

$$s =$$

$$t = 5$$

$$u = 0$$

$$v =$$

$$a = 9.8$$

$$s =$$

$$t = 1$$

$$s = (39.2)(5) - 4.9(25)$$

$$= 73.5$$

$$78.4 - 73.5 = 4.9$$

$$78.4 + 4.9 = 83.3 \text{ m}$$

$$s = 4.9(1)^2 = 4.9 \text{ m}$$

$$78.4 + 4.9 = 83.3 \text{ m}$$

2008
1 (b)

(* equal speeds shortest dist between them

120 sec.

P 23 m/s

P.

Q 5.5 m/s

Q 65.5 m/s

P: $u = 23$

Q: $u = 5.5$

$v =$

$v = 65.5$

$s = \left(\frac{5.5 + 65.5}{2} \right) 120$

$a =$

$a =$

$s = 4260 \text{ m}$

$s =$

$t = 120$

$t = 120 = 4260 \text{ m.}$

$4260 = 23(120) + a(7200) \Rightarrow a = \frac{5}{24} \text{ m/s}^2$

$v^2 = 23^2 + 2 \left(\frac{5}{24} \right) (4260)$

$65.5 = 5.5 + a(120)$

$60 = a(120)$

$\frac{1}{2} = a$
m/s²

$v^2 = 2304, v = 48 \text{ m/s}$

Moving at equal speeds:

P: $u = 23$

Q: $u = 5.5$

$v = v$

$v = v$

$a = \frac{5}{24}$

$a = \frac{1}{2}$

$s =$

$s =$

$t = t$

$t = t$

$v = 23 + \frac{5t}{24} = 5.5 + \frac{t}{2}$

$552 + 5t = 132 + 12t$

$420 = 7t$

$60 = t$

$S_p = 23t + \frac{5t^2}{48}$ $S_q = 5.5t + \frac{t^2}{4}$

$S_p - S_q = 17.5t - \frac{7t^2}{48}$

2007

(*) In 2nd Second etc.'

1(a): $u = u$

$u = u$

$v =$

$v =$

$a = 9.8$

$a = 9.8$

$s = x$

$s = x + 29.9$

$t = 2$

$t = 3$

$x = 2u + 4 \cdot 9(4)$

$x + 29.9 = 3u + 4 \cdot 9(9)$

$x = 2u + 19.6$

$x = 3u + 14.2$

$2u + 19.6 = 3u + 14.2$

$u = \cancel{2.3926} \quad 5.4 \text{ m/s}$

$u = 5.4$

$v =$

$a = 9.8$

$h = 5.4(4) + 4 \cdot 9(16)$

$s = h$

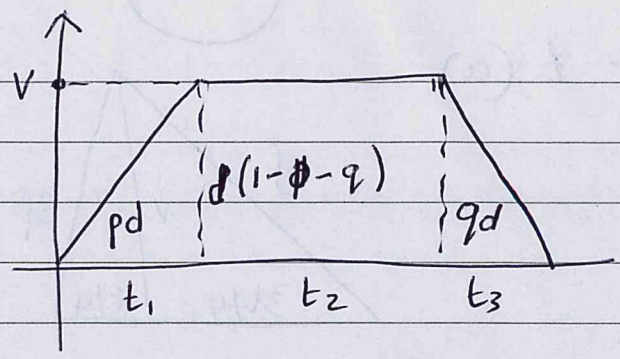
$h = 100 \text{ m}$

$t = 4$

2007 (*) def do (!!!)

1 (b.)

$u=0$
 $v=v$
 $a=$
 $s=$
 $t=$



$$\frac{d}{t_1 + t_2 + t_3} = \frac{v}{p + q + b} = \frac{d}{t} \quad pd + qd + bd = vt$$

$$\frac{\frac{t_1 v}{2} + \frac{t_2 v}{2} + \frac{t_3 v}{2}}{t_1 + t_2 + t_3} = \frac{v}{p + q + b}$$

$$vt_1 + vt_2 + vt_3 = pd + qd + bd$$

~~$\frac{vt_1}{2} + \frac{vt_2}{2} + \frac{vt_3}{2} = d$~~

$$\frac{d}{t} = \frac{v}{p + q + b}$$

$$vt = pd + qd + bd$$

$$vt_1 + vt_2 + vt_3 = pd + qd + bd$$

but $pd = \frac{vt_1}{2}$ so $2pd = vt_1$

$qd = \frac{vt_3}{2}$ so $2qd = vt_3$

and $vt_2 = d - pd - qd$ so

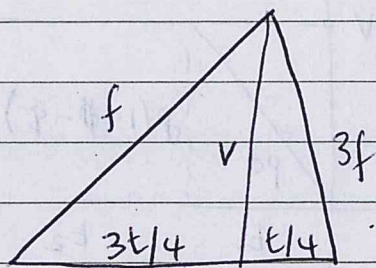
$$vt_1 + vt_2 + vt_3 = 2pd + 2qd + d - pd - qd$$

$$vt_1 + vt_2 + vt_3 = pd + qd + d = pd + qd + bd$$

so $b=1$

(* !!) Train lengths / passing

2006: 1 (a)



$$u = 0$$

$$v = v \quad v = \frac{3ft}{4}$$

$$a = f$$

$$s =$$

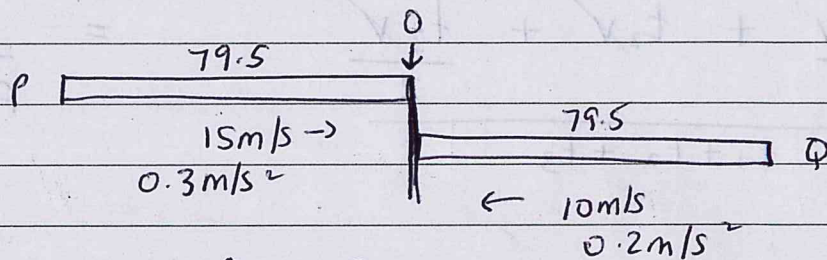
$$t = \frac{3t}{4}$$

$$d = \frac{1}{2}(t)(v)$$

$$d = \left(\frac{1}{2}\right)\left(\frac{3ft}{4}\right) = \frac{3ft^2}{8}$$

2006: 1 (b)

$$S_p + S_q = 159m$$



$$P: u = 15 \text{ m/s}$$

$$Q: u = 10$$

$$v =$$

$$v =$$

$$a = 0.3$$

$$a = 0.2$$

$$s = S_p$$

$$s = S_q$$

$$S_q = 10t + 0.1t^2$$

$$t = t$$

$$t = t$$

$$S_p = 15t + \frac{0.3t^2}{2} + S_q = 25t + 0.1t^2 = 159$$

$$2.5t^2 + 250t - 1590 = 0 \quad \text{182 secs}$$

$$25t^2 + 2500t - 15900 = 0 \quad t = 6 \text{ secs}$$

(iii) Can be done w/o (ii)

(*)

$$\frac{2}{5} \text{ of } 79.5 = v = 31.8 \text{ m}$$

$$u = 10$$

$$v =$$

$$a = 0.2$$

$$s = 31.8$$

$$t = ?$$

$$31.8 = 10t + 0.1t^2$$

$$0.1t^2 + 10t - 31.8 = 0$$

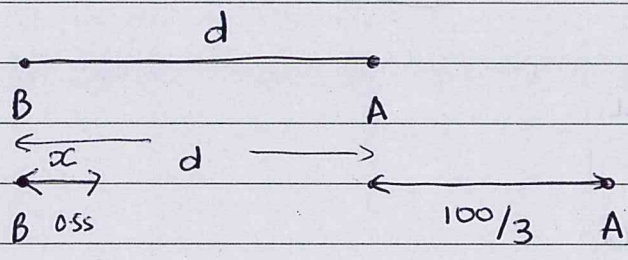
$$t^2 + 100t - 318 = 0$$

$$t = 3.08 \text{ s}$$

2005 1(a) (!!) V.I.P.

A: $u=20$
 $v=0$
 $a=-6$

$$s = \frac{0^2 - 400}{-12} = \frac{100}{3}$$



Car B not to collide means $x + \text{stopping distance} < \frac{100}{3} + d$

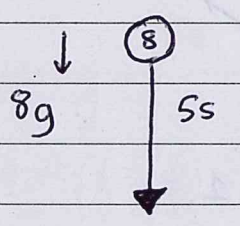
B's stopping distance : $u=20$
 $v=0$
 $a=-3$
 $s = \frac{0^2 - 400}{-6} = \frac{200}{3}$
 $t = \frac{0 - 20}{-3} = \frac{20}{3}$

$x = \text{what B travels in } 0.5s \text{ before he starts to brake:}$

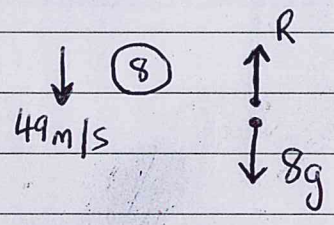
$$20 \times 0.5 = 10m \quad \text{so} \quad 10 + \frac{200}{3} < \frac{100}{3} + d$$

$$130/3 < d \quad d_{min} = 43.3$$

1(b) (!!!) V.I.P. (mass) (Force)



$u=0$ $v=0+9.8(5)$
 $v=$ $v=49m/s$
 $a=9.8$
 $s=$
 $t=5$



$u=49$ $0 = 49 - 0.01a$
 $v=0$ $\frac{49}{0.01} = a = 4900 m/s^2$
 $a=$ 0.01

$s=$ $F = ma = 39200N$
 $t=0.01$ $39200 = R - 8g$

$39200 + 8g = R$

$39278.4N = R$

(*) can do w/o previous!

$$s = \left(\frac{49+0}{2} \right) (0.01) = 0.245m$$

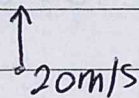
2004

Q1 (a)



Distance Vs Displacement

no assumptions!



$$u = 20$$

$$u = u$$

$$v =$$

$$v =$$

$$a = -9.8$$

$$a = -9.8$$

$$s = s$$

$$s = s$$

$$t = 3$$

$$t = 2$$

~~$$t^2 \leq 6t + 9$$~~

~~$$s = 20t - 4.9t^2$$~~

~~$$s = ut - \frac{1}{2}at^2 + v(4.9)t - 9t$$~~

~~$$20t - 4.9t^2$$~~

~~$$= ut - 3u - 4.9t^2 + 29.4t - 44.1$$~~

~~$$20t = ut - 3u + 29.4t - 44.1$$~~

$$s = 60 - 4.9(9)$$

$$s = u(2) - 4.9(4)$$

$$= 60 - 44.1 = 15.9 \text{ m}$$

$$= 2u - 19.6$$

$$35.5 = 2u$$

$$17.75 = u$$

Distance travelled : Ball 2 = 15.9m?

Ball 1 = ?

need to find greatest height for ball 1 :

$$u = 20$$

$$s = 400 - 19.6s$$

$$v = 0$$

$$a = -9.8$$

$$\frac{400}{19.6} = s = 20.41$$

$$s = s$$

$$19.6$$

$$t = ?$$

$$20.41 + 20.41 - 15.9$$

$$= 24.92 \text{ m} \quad (25)!$$

Ball 2 : $u = 17.75$

$$v = 0$$

$$s = \frac{17.75^2}{2(9.8)} s$$

$$a = -9.8$$

$$s = 16.07$$

$$s =$$

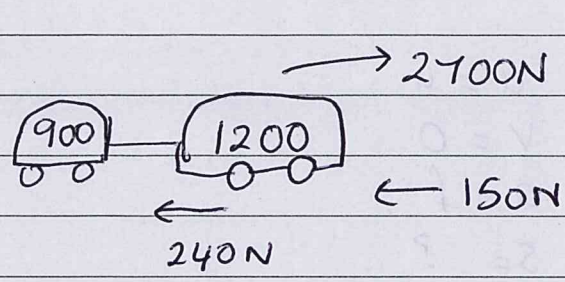
$$s = 16.07 + 16.07 - 15.9 = 16.24$$

$$t =$$

(16)!

2000 1 (b) (!!!) Force!
Q

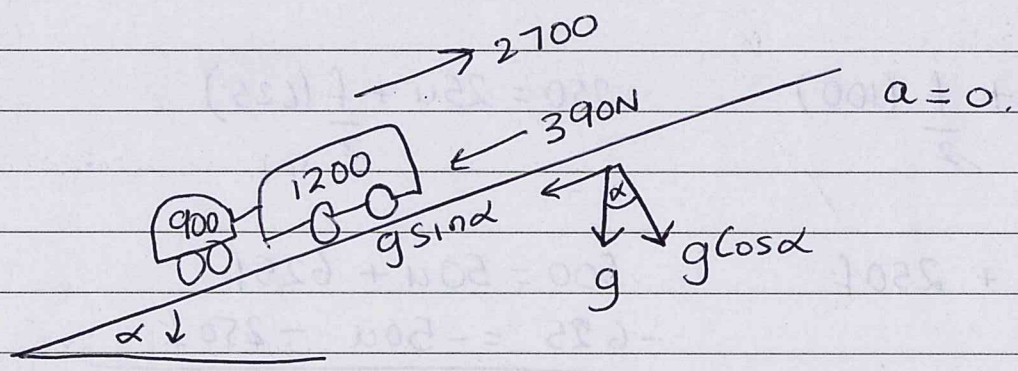
(Uniform Speed !!!)
F=0



$$F = 2700\text{ N} - 390\text{ N}$$

$$F = 2310\text{ N}$$

$$f = \frac{2310}{2100} = 1.1\text{ m/s}^2$$



$$390 + 2100g \sin \alpha = 2700 \quad 2100g \sin \alpha = 2310$$

$$\sin \alpha = \frac{2310}{2100g} = 0.1122$$

$$\alpha = 6.44^\circ$$

Uniform speed up hill!

2003: Q1 (a) V.I.P. Passing posts (!!) (*)

$u = u$	$u = u$	$u = u$
$v =$	$v =$	$v = 0$
$a = f$	$a = f$	$a = f$
$s = 125$	$s = 250$	$s = ?$
$t = 10$	$t = 25$	$t =$

(i)

$$125 = 10u + \frac{f}{2} (100)$$

$$250 = 25u + \frac{f}{2} (625)$$

$$625 = 50u + 250f$$

$$500 = 50u + 625f$$

$$\underline{-625 = -50u - 250f}$$

$$-125 = 375f$$

$$-1/3 = f, \quad 10u = 125 + \frac{50}{3}$$

$$u = 14.1\bar{6} \text{ m/s} = \frac{425}{3}$$

(ii) $u = u = 14.1\bar{6} \text{ m/s}$

$$v = 0$$

$$a = f = -1/3$$

$$s =$$

$$t =$$

$$s = \frac{425}{3} \times 10$$

$$0 = \left(\frac{425}{3}\right)^2 - 2\left(\frac{1}{3}\right)s$$

(*) Ans the Q!!!
or (-5 marks)

$$s = \left(\frac{425}{3}\right)^2 \times \frac{3}{2} = 301.04 \text{ m}$$

$$\text{Ans: } 301.04 - 250 = 51.04$$

1(b) (!!!) Closest distance (!!) (*)

$S_m = vt = 20v$ $S_{bus} = ?$ $u = 0$
 $v = \frac{1}{2} V_m$
 $a =$
 $s =$
 $t = 20$

$S_m = 40 = S_{bus}$ $S_{bus} = \left(\frac{0 + v}{2}\right) 20$
 $20v - 40 = 10v$ $S_{bus} = 10v$

$10v = 40 \Rightarrow v = 4 \text{ m/s}$ $a = 1/5 \text{ m/s}^2$

(!) use a from (i)

(ii) $S_{man} = 3t$ $S_{bus} = ?$ $u = 0$
 $v = V = 3$
 $a = 1/5 \text{ m/s}^2$
 $s = vt/2 = 3t/2$
 $t = t$

$S_{man} = 3(15) = 45 \text{ m}$ $3 = 0 + t/5 \Rightarrow t = 15 \text{ secs}$

$S_{bus} = 45/2 = 22.5$

$S_{between} = 45 + 22.5 + 40 = 17.5$

~~$S_{man} - S_{bus} + 40$~~ OR $S_{between} = S_b + 40 - S_m$

$3t - \left(\frac{1}{5} \left(\frac{1}{2}\right) t^2 + 40\right) = \text{max}$ $= 40 + \frac{t^2}{10} - 3t$ (different)
 $3t - \frac{1}{10} t^2 + 40 = \text{max}$ $\frac{2t}{10} = 3t \Rightarrow t = 15$
 $3t - \frac{t^2}{10} + 40 = \text{max}$ $-\frac{t}{5} = 3 \Rightarrow t = 15$
 17.5 m

(∴) negative displacement

2002: Q1 (a.)

$$u = u$$

$$v = -30 = 5u - 4.9(25)$$

$$a = -9.8$$

$$s = -30 \quad 5u = \frac{185}{2}$$

$$t = 5 \quad u = 18.5$$

$$v = 18.5 - 9.8(5)$$

$$v = -30.5 \downarrow$$

2002 Q1(b) Passing posts (!!)(!)

$$u = u$$

$$u = a$$

$$u = u$$

$$v =$$

$$v =$$

$$v =$$

$$a = a$$

$$a = a$$

$$a = a$$

$$S = p$$

$$S = q + p$$

$$S = q + p + r$$

$$t = t$$

$$t = 2t$$

$$t = 3t$$

$$p = ut + \frac{at^2}{2}$$

$$q + p = 2ut + \frac{a(4t^2)}{2}$$

$$p = ut + \frac{at^2}{2}$$

$$q + p = 2ut + 2at^2$$

$$q + p + r = 3ut + \frac{9t^2}{2}$$

$$q = 2ut + 2at^2 - ut - \frac{at^2}{2} = \frac{ut + 3at^2}{2} = q$$

$$2q = 2ut + 3at^2$$

$$r = 3ut + \frac{9at^2}{2} - 2ut - 2at^2 = \frac{ut + 5at^2}{2} = r$$

$$2q = p + r?$$

$$2ut + 3at^2 = ut + \frac{at^2}{2} + ut + \frac{5at^2}{2}$$

$$= 2ut + 3at^2 \checkmark$$

(ii)

$$u = u$$

$$v =$$

$$a = a$$

$$S = p + q + r + x$$

$$t = 4t$$

$$p + q + r + x = 4ut + \frac{a(16t^2)}{2} = 4ut + 8at^2$$

$$x = 4ut + 8at^2 - 3ut - \frac{9at^2}{2} = 4ut + \frac{7at^2}{2} = 2r - q$$

$$\begin{array}{r}
 2r = 6ut + 9at^2 \\
 - q = -2ut - 3/2 at^2 \\
 \hline
 4ut - 7/2 at^2
 \end{array}$$

$$2r = 2ut + 5at^2$$

$$q = ut + \frac{3at^2}{2}$$

$$2r - q = \frac{4ut + 7at^2}{2} = x$$

$$p = \frac{ut + 3at^2}{5}$$

$$r = \frac{ut + 3at^2}{5}$$

$$3r = \frac{3ut + 9at^2}{5}$$

$$3r = 3ut + 9at^2$$

$$p + r = \frac{2ut + 6at^2}{5} = 4ut + 8at^2$$

$$p - r = \frac{2ut + 6at^2}{5} = 3ut + 6at^2$$